

Ionisation in atmospheres of Brown Dwarfs and extrasolar planets

III. Breakdown conditions for mineral clouds

Ch. Helling¹, M. Jardine¹, C. Stark¹, D. Diver²,

1: SUPA, School of Physics & Astronomy, University of St Andrews, St Andrews, KY16
9SS, UK

2: SUPA, School of Physics and Astronomy, University of Glasgow, Glasgow G12 8QQ, UK

ch@leap2010.eu

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ABSTRACT

Electric discharges were detected directly in the cloudy atmospheres of Earth, Jupiter and Saturn, are debatable for Venus, and indirectly inferred for Neptune and Uranus in our solar system. Sprites (and other types of transient luminous events) have been detected only on Earth, and are theoretically predicted for Jupiter, Saturn and Venus. Cloud formation is a common phenomenon in ultra-cool atmospheres such as in Brown Dwarf and extrasolar planetary atmospheres. Cloud particles can be expected to carry considerable charges which may trigger discharge events via small-scale processes between individual cloud particles (intra-cloud discharges) or large-scale processes between clouds (inter-cloud discharges). We investigate electrostatic breakdown characteristics, like critical field strengths and critical charge densities per surface, to demonstrate under which conditions mineral clouds undergo electric discharge events which may trigger or be responsible for sporadic X-ray emission. We apply results from our kinetic dust cloud formation model that is part of the DRIFT-PHOENIX model atmosphere simulations. We present a first investigation of the dependence of the breakdown conditions in Brown Dwarf and giant gas exoplanets on the local gas-phase chemistry, the effective temperature and primordial gas-phase metallicity. Our results suggest that different intra-cloud discharge processes dominate at different heights inside mineral clouds: local coronal (point discharges) and small-scale sparks at the bottom region of the cloud where the gas density is high, and flow discharges and large-scale sparks near, and maybe above, the cloud top. The comparison of the thermal degree of ionisation and the number density of cloud particles allows us to suggest the efficiency with which discharges will occur in planetary atmospheres.

Subject headings: Brown Dwarfs, atmospheres, dust, ionisation, magnetic coupling

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1. Introduction

Electric discharges, including transient luminous events¹ or transient discharges in gases, are non-equilibrium plasmas produced by short-lived electrical conditions of which lightning and associated sprites are the most widely known. Lightning and sprites are commonly observed on Earth. Lightning is also detected or indirectly inferred on most of the cloud-carrying solar system planets. Observations on Earth show that cloud particles or droplets trigger such transient discharges in atmospheric environments (e.g. Yuan et al. 2011). It is not obvious that the underlying physical mechanisms for triggering lightning and sprites are different: they each involve an unbalanced evolution of accelerated free electron populations, driven by electric potential differences. How the latter are created from the organisation of ambient gas/particles may be different, but the underlying science is not.

Most of the solar system planets form clouds made of liquids and ices, but dependent on local conditions, mineral hazes may also form (e.g. Saunders & Plane 2011). Recent observations of HD 189733b (Pont et al. 2008; Sing et al. 2009, 2011; Gibson et al. 2012) suggest that extraterrestrial giant gas planets contain small mineral dust particles high up in their atmospheres. Further examples include GJ1214b and Kepler 7b.

Prompted by the abundance of discharge processes in clouds on Earth and in the clouds of solar system planets, we take a first look at the conditions for such discharge events in extrasolar, planetary and Brown Dwarf atmospheres. The essential requirements

¹In the community of terrestrial atmospheric physics, the term *transient luminous event* is used to describe sprites, elves, and blue-jets only, but not lightning.

are the presence of both, an electric field (electric potential difference) and free electrons. This electric field accelerates the free electrons through the ambient gas. If they collide with other gas particles sufficiently frequently and with enough energy to liberate increasingly more electrons, an electron avalanche is produced. The critical electric field required for this depends, to some extent, on the composition of the gas. This avalanche can develop into a self-propagating ionisation front (streamer) if the self-field of the electrons in the avalanche is similar to the strength of the applied external field. If the avalanche has reached a critical size, it can propagate into areas with a lower electric field strength in which an avalanche would not start normally. Two electrical breakdown mechanisms are known to occur in dielectrics: the conventional breakdown occurring for example in glow discharges; and the runaway breakdown which is suggested to play a role in lightning discharges on Earth. The threshold electric field needed to initiate the avalanche of a runaway breakdown appears one order of magnitude below that for a conventional breakdown (for more details see Roussel-Dupre et al. 2008; Marshall et al. 1995). Each of the resulting streamers is a highly conducting plasma channel in which the density of non-thermal electrons is greatly increased, and from which electrons leak into the ambient gas.

Helling, Jardine & Mokler (2011) have argued that dust clouds that are made of mineral particles can be charged e.g. by gas turbulence induced dust-dust collisions. The cloud particles remain charged for long enough that discharge events can occur and streamers can be established. Other possible processes for charge separation, which we have not considered, are e.g. different contact potentials of the material making up the grain, and fractoemission or collisional charging of polarised grains in an external electric field (Pähtz, Herrman & Shinbrot 2010). The Coulomb recombination time of cloud particles by thermal electrons is long enough that electric fields can establish between passing grains which then can initiate subsequent electron avalanche processes leading to streamers (Fig. 4 in Helling et al. 2011). The result is that during the electron avalanche phase there is

an exponential increase in free charges for each free electron that exists in the gas phase. Numerical experiments that simulate an avalanche from the initial electron up to and beyond the avalanche-to-streamer transition demonstrate consistently that a single electron seeding a streamer can cause the occurrence of $10^{12} - 10^{13}$ secondary non-thermal electrons for a certain time interval (Dowds et al. 2003, Ebert et al. 2010).

Laboratory studies suggest that during grain-grain impact, smaller grains are more negatively charged compared to larger grains of the same composition (Lacks & Levandovsky 2007, Forward et al. 2009, Merrison et al. 2012). A similar conclusion was reached from volcano ash experiments (Hatakeyama & Uchikawa 1952, Kikuchi & Endoh 1982, James et al. 2000). Experimental results for different minerals are not available at present. Experiments on wind-driven entrainment of Martian dust (mainly iron oxides) and Basalt dust (Na/K/Ca-silicates) by Merrison et al. (2012) suggest average electric charge values of $10^3 \dots 10^5 \text{ e}^-/\text{grain}$. The exact values might, however, be influenced by the experimental set-up (Aplin et al. 2012). These experiments were carried out under pressures between 10 mbar and 1 bar. Only a very weak pressure dependence on the number of charges per grain was seen. No strong dependence on the grain material was found either, but one order of magnitude variation is suggested due to grain sizes, morphology and abundance of grains. They found no evidence for a dependence of dust electrification on atmospheric composition.

The extrasolar atmospheric environments we are looking at in Brown Dwarfs and giant gas planets have local temperatures between $T_{\text{gas}} = 500\text{K} - 4000\text{K}$ and gas pressures between $p_{\text{gas}} \approx 10^{-10}\text{bar} - 10 \text{ bar}$. This pressure range comprises the pressure interval for Mars-dust analog experiments by Merrison et al. (2012). The resulting degree of ionisation by thermal processes in Brown Dwarfs and giant gas planet atmospheres is $\chi_e = p_e/p_{\text{gas}} \approx 10^{-15} - 10^{-7}$ throughout the atmosphere, which is very low (Helling et al. 2012), but enough to

start an electron avalanche. The formation of dust by seed formation and bulk growth takes place in a temperature window of $\sim 500\text{K} - \sim 2100\text{K}$ and leads to the formation of mineral clouds. Gravitational settling, convective mixing and element depletion are major associated processes. Helling, Woitke & Thi (2008) have shown that the upper cloud, (i.e. low temperature and low-pressure) will be dominated by small, dirty (i.e. inclusions of other materials) silicate grains with inclusions of iron and metal oxides, and the warmer, denser cloud base by bigger, dirty iron grains with metal inclusions. The actual size of the cloud particles deviate from this mean value according to a height dependent size distribution (Fig. 8 in Helling, Woitke & Thi 2008). The chemical composition of the grains as well as their size distribution change with height inside a cloud in a quasi-stationary environment.

The different scale regimes involved in the formation of atmospheric clouds suggest the consideration of two different scale regimes with respect to charge and discharge processes. The large scale regime is where the cloud particles settle gravitationally (rain out) according to their mass and size, or where they are transported by hydrodynamical processes like convection. This will leave the smallest and potentially more negatively charged particles suspended in the higher layers, while the larger and more positively charged particles populate the lower part of the cloud. The small scale regime describes the scales at which cloud particles interact during grain-grain collisions, where colliding particles (droplet) or individual cloud particles produce point discharges (also called *corona*) that may start large-scale lightning. This analogy is drawn from the discharge experiments for Earth conditions where colliding drops in storms and ice particles can produce point discharges which are thought to be able to initiate lightning (for more details see MacGorman & Rust 1998). A similar scenario is suggested in Merrison et al. (2012), and was utilised by Farrell et al. (1999) and Michael et al. (2008) to model Martian dust storms.

What are the conditions to trigger a discharge event which subsequently increases the

local density of free electrons by non-thermal processes leading potentially to the occurrence of lightning or associated transient luminous events like sprites? The local electric field, E , must exceed the ionisation threshold of the ambient gas, hence a critical field strength, E_{crit} , and seed electrons for the development of an electron avalanche need to be present. We note that measurements of the actual threshold electric field strength for a terrestrial lightning flash in a cloud are not easy to obtain (Marshall et al. 2005). Marshall et al. (1995) performed balloon experiments from which they derived electric breakdown thresholds that led them to hypothesised that lightning flashes might be initiated by runaway breakdown. This paper therefore presents a first investigation of the discharge behaviour in extrasolar atmospheres by studying the following questions.

- What electric field strength is needed to allow breakdown phenomena known from Earth and solar system planets to occur in extrasolar, planetary objects and Brown Dwarfs?
- What can we learn about the breakdown conditions in extrasolar objects, for example breakdown distances, minimum voltages, or chemistry dependence?
- What are the critical conditions for breakdown such as cloud size, grain size, number of charges per surface? Under which conditions can the critical field strength be produced by grains alone?
- How many thermal electrons are available in a mineral cloud of a Brown Dwarf or a giant gas planet in order to trigger a streamer event? How efficiently can discharge events occur and, hence influence the gas phase composition?

To answer these questions, we first outline the basic ideas and relations for an electrostatic breakdown in gases of different chemical compositions in Sect. 2. These relations are evaluated in Sect. 3 for previously calculated model atmosphere structures of Brown Dwarfs and giant gas planets. We are using DRIFT-PHOENIX model atmosphere structures which are the result of the solution of the coupled equations of radiative transfer, convective energy transport (modelled by mixing length theory), chemical equilibrium

(modelled by laws of mass action), hydrostatic equilibrium, and dust cloud formation (Dehn 2007, Helling et al. 2008a,b; Witte, Helling & Hauschildt 2009; Witte et al. 2011). The dust cloud formation model includes a model for seed formation (nucleation), surface growth and evaporation of mixed materials. The effects of gravitational settling (drift) and convective overshooting on the cloud formation are explicitly included in our dust model equations (Woitke & Helling 2003, 2004; Helling & Woitke 2006; and Helling, Woitke & Thi 2008). The results of the DRIFT-PHOENIX model atmosphere simulations include for example the gas temperature - pressure structure (T_{gas} , p_{gas}), the local gas-phase composition, the local electron number density (n_e), the number of dust grains (n_d) and their height dependent sizes (a). These models are determined by the effective temperature, T_{eff} [K], the surface gravity, g [cm/s²], and the initial element abundances which are set to the solar values unless specified otherwise. The final element abundances are determined by element depletion due to dust formation. We also discuss how many charges per surface would be needed to initiate a field breakdown based on this model output (Sect. 3.2), and we estimate the enrichment rate of the gas-phase by streamer electrons (Sect. 3.4). Section 4 contains our conclusions.

2. Breakdown characteristics

Electric breakdown is the process of transforming a non-conducting substance into a conductor as the result of applying a sufficiently large electric field. This ionisation state of the bulk gas phase builds up over times between $10^{-8} \dots 10^{-4}$ s and is large enough that it is accompanied by a light flash. A gas-phase breakdown is a threshold process, hence, it occurs when the local electric field exceeds a value characteristic of the special local conditions.

A streamer develops in the wake of a positively charged tail of a primary avalanche

during which an accelerated electron travels through an ambient gas. If the energy of the accelerated electron exceeds the ionisation potential of the gas, the growth of a thin ionisation channel (streamer) between two electrodes results. These electrodes can be capacitor plates, charge distributions inside clouds, or grains. The transition between an avalanche process and the streamer mechanisms is not well documented so far. Raether (1964) suggests that the streamer mechanism dominates at an electrode distance of 5-6 cm, the exact value of which might change depending on local conditions.

The onset of electric field breakdowns has been studied for charge distributions on capacitor plates for a variety of gases and characteristic quantities, and the breakdown voltage has been parametrised for easy use based on lab experiments (Eq. 1- 2; e.g. Raizer 1991). Different electric field strengths inside a capacitor were tested for different gases. For practical reasons, the parametrisation of the breakdown voltage has only been done for terrestrial or solar system gas mixtures or for homogeneous gases, which may not resemble the gas composition in an extrasolar planetary or Brown Dwarf atmosphere.

The resulting Paschen curve, that relates the breakdown voltage with the product pd (Eqs. 1, Fig. 1), shows that the breakdown voltage of a capacitor, V_t [V], depends only on the material of the cathodes (characterised by Townsend’s second ionisation coefficient γ), the gas between the capacitor plates (characterised by the coefficients A [$\text{cm}^{-1} \text{ torr}^{-1}$] and B [$\text{V cm}^{-1} \text{ torr}^{-1}$]), and the product between the gas pressure and the capacitor plate separation, pd [cm torr],

$$V_t = \frac{B \cdot pd}{C + \ln(pd)} \quad \text{with} \quad C = \ln \frac{A}{\ln(\frac{1}{\gamma} + 1)} \quad (1)$$

$$\frac{E_t}{p} = \frac{B}{C + \ln(pd)} \quad (2)$$

Townsend’s second ionisation coefficient γ is the effective secondary emission coefficient of the cathode and can be calculated as the ratio between the number of electrons ejected per incident ion. We will refrain from doing so and apply numbers given in the literature. γ

varies between 10^{-9} for organic cathode materials and 10^{-2} for nickel and copper cathodes (Table 4.10 in Raizer 1991). If $\gamma = 1$ there is one ionisation event per hit. However, the breakdown voltage becomes independent of the cathode material when a spark breakdown or a streamer starts to develop. This is evident from the fact that lightning in Earth is not triggered by electron emission of the cloud ‘cathodes’, the negatively charged part of a cloud.

Qualitatively, the Paschen curve predicts that the breakdown voltage decreases as the electrode gap decreases because the corresponding electric field increases. The Paschen curve proved to be accurate for large gaps and low pressures but it is observed to fail at extremely low and high pd -values. We note that experiments show that the Paschen curve is not necessarily accurate in describing breakdowns between electrode spaces of less than $15\mu\text{m}$. Go & Pohlman (2010) have therefore derived a model for a modified Paschen curve for breakdown in micro-scale gaps. In their model, the breakdown voltage does not have a singularity ($+\infty$) for small gap sizes but instead decreases further (see their Fig.1). The observation that $pd = \text{const}$ does not hold for small gaps, and p and d become independent variables. For the small-scale cases considered, i.e. the distance between two charge centres in the form of grains, the gap size is just large enough to allow us to apply the classical Paschen curve formalism (Fig. 2).

At some gap size, the classical Paschen curve has a minimum, the Stoletow point, which is calculated from $dV_t/d(pd) = 0$, resulting in

$$pd = \frac{e}{A} \ln\left(\frac{1}{\gamma} + 1\right). \quad (3)$$

pd is a local constant for a given gas composition (expressed by the constants A , B) and for a given capacitor surface material (expressed by the Townsend’s second ionisation coefficient γ) as long as the gap d is large enough. The product pd will therefore be the same for any planet or Brown Dwarf given they have the same gas composition. The capacitor plate

distance, d , which in our small-scale case is the distance between passing grains, changes with the local gas pressure, which in our case is a proxy for the vertical position in the atmosphere (Fig. 2).

Figure 1 shows $V_t(pd)$ with the Stoletow point of these gas-chemistry dependent Paschen curves indicated by octaeder symbols. Brown dwarfs would be best represented by the Paschen curve for H_2 (brown dashed line) and giant gas planets will very likely exhibit a more complex gas-phase composition because they form from a protoplanetary disk at different distances from the host stars therein. The minimum breakdown voltage $V_{t,\min}$ [V] follows by inserting Eq. 3 into Eq. 1 (left),

$$V_{t,\min}(pd) = \frac{e^1 B}{A} \ln\left(\frac{1}{\gamma} + 1\right). \quad (4)$$

Thus, for each gas composition, there is a minimum voltage required to achieve electric breakdown in the gas. Only then can a streamer or subsequent lightning develop. It may however be more useful to express this condition in terms of the electric field strength \vec{E} . With $E = |\vec{E}| = |-\partial\phi(r)/\partial r|$, and $\phi(r)$ the electric potential and voltage $V = \Delta\phi(r)$ being the potential difference (Δ) between two points (hence, the units are the same), it follows $E = V/r$ for a spherical charge distribution at a radial distance r from the charge Q ($E = V/d$ for a capacitor). Inserting Eq. 3 into Eq. 2, the breakdown or ignition field strength follows with $E = |-\partial\phi/\partial r|$ from the following relation

$$\frac{E_{t,\min}}{p} = B \quad \Rightarrow \quad E_{t,\min} = Bp. \quad (5)$$

Hence, $(E_{t,\min}/p)=\text{const}$ is a universal constant of a gas in the capacitor or the gas exposed to the electric field of some charge distribution. $E_{t,\min}$ is the minimum electric field strength needed to achieve breakdown. Raizer (1991) and Sentman (2004) have published $(E_{t,\min}/p)$ -values for various gases and gas mixtures potentially representative of the solar system planetary atmospheres. These values are based on either experiments or calculations

that take into account details of the interaction processes of the electron with the ambient gas. For example, Sentman (2004) deals with gas mixtures by Boltzman modelling of the electron distribution function for a given gas composition (added to Table 1). Hence, details on the acceleration process, scattering and energy losses/gains are ‘hidden’ in the measured material constant. A detailed review of a kinetic approach can be found in Roussel-Dupre et al. (2008). We summarise the values in Table 1 as some of the original literature is hard to come by. For more details on composition dependencies consult Chapter 6 in Meek & Craggs (1978).

In summary, once the gas composition is defined for a given Brown Dwarf or gas giant planet, the pressure variation with height defines the variation of the minimum electric field needed for breakdown in the atmosphere which we will investigate in more detail below.

3. Results

The breakdown quantities introduced in the previous section will now be evaluated for a set of atmosphere structures that were previously calculated using the DRIFT-PHOENIX model atmosphere code by Witte, Helling & Hauschildt (2009). These model atmospheres provide the required input quantities for the following calculations which are the local gas pressure, p_{gas} , and grain sizes, a , for each height in the atmosphere. Two models are studied in detail: $T_{\text{eff}} = 1600\text{K}$, $\log(g)=5.0$ as the example for a Brown Dwarf atmosphere, and $T_{\text{eff}} = 1600\text{K}$, $\log(g)=3.0$ as the example for a non-irradiated giant gas planet. Both atmospheres have an initially solar metallicity. Later in the paper, we compare these results to models of different effective temperature $T_{\text{eff}} = 1600, 1900, 2100, 2500\text{K}$ and 2800K (Fig. 8), and the initial metallicity is varied between $[M/H] = -5 \dots 0$ with $[M/H]=0$ indicating the solar values (Fig. 9). The comparison amongst these models allows us to identify trends in the electric breakdown quantities in substellar and low-metallicity

Table 1: Parametrisation of electric breakdown field according to Paschen curves: Material constants A & B taken from Raizer (1991) and from Sentman (2004), pd and $V_{t,\min}$ calculated from Eqs. 3, 4. $\gamma = 0.001$

	A	B	pd_{\min}	$V_{t,\min}$
	[1/(cm Torr)]	[V/(cm Torr)]	[cm Torr]	[V]
	(Raizer 1991)	(Raizer 1991)	(this paper)	(this paper)
He	3	34	4.181	142.2
H ₂	5	130	2.509	326.1
N ₂	12	342	1.045	357.5
Air	15	365	0.8363	305.2
CO ₂	20	466	0.6272	292.3
H ₂ O	13	290	0.9649	279.8
	A	E/p=B	pd_{\min}	$V_{t,\min}$
Sentman (2004)	[1/(cm Torr)]	[V/(cm Torr)]	[cm Torr]	[V]
Venus (CO ₂ /N ₂ =96.5/3.5)	7.27	180	2.58	465
Earth (N ₂ /O ₂ /Ar=78/21/1)	7.44	243	2.53	617
Mars (CO ₂ /N ₂ /Ar=95.5/2.8/1.7)	7.23	178	2.60	462
Jupiter (H ₂ /He/CH ₄ =89/10.9/0.1)	6.19	143	3.06	434
Saturn (H ₂ /He/CH ₄ =96.3/3.6/0.1)	7.46	156	2.52	392
Titan & Tritan (N ₂ /CH ₄ =95/5)	8.80	274	2.13	585
Uranus (H ₂ /He/CH ₄ =82.5/15.2/2.3)	6.47	138	2.90	401
Neptune (H ₂ /He/CH ₄ =80/18.5/1.5)	622	135	3.02	408

atmospheres.

3.1. Classical breakdown quantities

Breakdown distance d : Assuming that a charge separation has built up in a Brown Dwarf or planetary atmosphere, how far can two imaginary capacitor plates be apart that a breakdown of the atmospheric gas will occur for an established electric field?

This is the distance of two capacitor plates, or two otherwise charge-carrying surfaces, that can build up an electric field between them, as described by the Paschen minimum where $p_{\text{gas}} \cdot d = 2.509 \text{ torr cm}$ ($=5007 \text{ dyn/cm}^2$) for an H_2 gas (Eq. 3, Fig. 1). This is the distance where the electrical breakdown would be easiest according to Eq. 4. Hence, for $p_{\text{gas}} \cdot d$ below the Paschen minimum, the breakdown voltage increases sharply in the classical case. However, Go & Pohlman (2010) show that lower breakdown voltages should be expected at smaller distances, justifying our use of the classical Paschen curve as a first step to study breakdown characteristics. $p_{\text{gas}} \cdot d$ is a constant for a given A [$\text{cm}^{-1} \text{ torr}^{-1}$] and γ , hence, the same for all atmospheres of the same chemical composition with respect to the most abundant gas-phase species. This allows us to calculate the breakdown distance d for a known p_{gas} -structure of a model atmosphere.

Figure 2 shows the breakdown distance as function of the local gas pressure calculated for the pressure structure of a Brown Dwarf ($T_{\text{eff}} = 1600\text{K}$, $\log(g)=5.0$, solar element abundances, brown line) and a giant gas planet ($T_{\text{eff}} = 1600\text{K}$, $\log(g)=3.0$, solar element abundances, red lines) assuming that molecular hydrogen ($A[\text{H}_2]=5 \text{ cm}^{-1}\text{Torr}^{-1}$, Raizer 1991) is the dominating gas species to be ionised by electrons accelerated in the electric field. This assumption is appropriate as H_2 is the most abundant molecule in the atmosphere models applied here. The assumption breaks down if H_2 ionises in the hot and dense inner

layers of the atmosphere where clouds can not be thermally stable, and where atomic hydrogen is the dominating gas component. The Townsend’s 2nd ionisation coefficient $\gamma = 0.001$ is used, representing a conducting cathode material which is strictly correct only for $T > 1800\text{K}$ from which iron dominates the grain material composition in the cloud. As mentioned earlier, it is only relevant to consider the material dependence of γ for the avalanche process, not so for the streamer.

Figure 2 shows that the breakdown distance varies over the atmosphere pressure ranges from $\sim 5\mu\text{m}$ in the densest regions to 10^5km in the upper, low pressure regions (dashed lines). This suggests that discharges could appear spatially extended and diffuse in low-pressure regions, while numerous discharge events remain small, locally confined phenomena in high-pressure regions. It also suggests that different electric discharge processes dominate at different heights: local corona (point discharges) and small-scale sparks at the bottom of the cloud, and glow discharge and large-scale sparks at the top.

In a quasi-static environment, these different processes could lead to a neutralisation of large-scale charge built-up and consequently diminish the possibility for a large-scale lightning. However, hydrodynamic atmosphere motions are driven by convection and by gravity waves (Freitag et al. 2010) on Brown Dwarfs which are also rapid rotators (Scholz et al. 2011). This suggests that large-scale charge separation is likely to be sustained by convection-like processes comparable to Earth, for example like in the Hadley cells at the Earth’s equator.

Following the observation in Raizer (1991) that for breakdown distances $> 5 \dots 6\text{cm}$ the streamer mechanism will dominate and sparks can develop, we distinguish a large-scale ($d > 6\text{cm}$) and a small-scale regime ($d < 6\text{cm}$) in Fig 2.

It is interesting to compare the maximum spacial separation that two charge distributions whilst still permitting a discharge, to the average size of the cloud particles

and their mean particle distance. For simplicity, we consider the altitude dependent mean grain size $\langle a \rangle$ instead of separate grain size distributions for each altitude as shown in Helling, Woitke & Thi (2008). The mean grain size, $\langle a \rangle$, is always smaller than the maximum distance, d , over the whole geometrical extension of the cloud. The mean distance between the cloud particles scales with the cloud particle number density as $n_d^{-1/3}$. Consequently, it will be largest where the number density is smallest. The 'knee' at the high-pressure end of each long-dashed curve in Fig. 2 corresponds to the maximum cloud particle number density (compare the upper panel in Fig. 10). Generally, the cloud particles have a mean separation that is ~ 3.5 orders of magnitude smaller than the maximum break-through distance in a giant gas planet cloud (~ 2.5 for the Brown Dwarf cloud). This comparison also shows that the cloud particles have considerable separation in the upper cloud region suggesting that collective phenomena such as large-scale charge distributions are to be expected rather than inter-particle discharges such as in the high-pressure part of the cloud. However, if the breakdown distance is smaller than the maximum value d (e.g. in a turbulent flow), small-scale discharge processes may also occur in the low-pressure part of an atmosphere.

Note, the mean particle size and the cloud particle number density are determined by the processes of dust and cloud formation (nucleation, growth/evaporation, drift, convective mixing, element depletion) taken into account in the DRIFT-PHOENIX model atmospheres. Coagulation, for instance, could change the grain size distribution, but it is not clear *a priori* how it changes since a variety of constructive and destructive collisional processes occur (Güttler et al. 2010). Furthermore, turbulence (Helling et al. 2001, 2004) and gravity waves (Freytag et al. 2010) cause local, hydrodynamic density increases, neither of which is taken into account in the present paper.

Depending on the ionising gas, these global values of d have uncertainties of one

order of magnitude as we demonstrate for different gas-phase compositions in Fig. 3. The breakdown distances inside the cloud regions (solid lines, Fig. 2) are somewhat different in a Brown Dwarf mineral cloud and in a giant planet’s mineral cloud because the Brown Dwarf clouds exist at higher pressures. The exact values of discharge quantities, such as the maximum separation of charge distributions before breakdown but also the required number of charges, will therefore differ between objects of different effective temperature, surface gravity and metallicity (see Figs. 8, 9).

Minimum electric field for breakdown $E_{t,\min}$: The minimum electric field strength, needed for a gas breakdown scales with the local gas pressure (Eq. 5), are shown in Fig. 4. This critical breakdown field strength corresponds to the minimum of the Paschen curve for individual ionised gases (H_2 , He, air, H_2O , CO_2 ; Table 4.1 in Raizer 1991) represented by individual parameters B [$V\text{ cm}^{-1}\text{ torr}^{-1}$], and a given Townsend’s 2nd ionisation coefficient $\gamma = 0.001$. The results are shown for a sample model atmosphere ($T_{\text{eff}}=1600\text{K}$, $\log(g)=5$, initial solar composition) for which we vary the parameter B to show the dependence on gas composition. Figure 4 shows results for pure gases (data from Raizer 1991), and Fig. 5 for mixed gases of the solar system planets (data from Sentman 2004). Over-plotted in Fig. 4 are the values given in Yair et al. (1995: magenta - Jupiter cloud with drops and ice, cyan - Earth values; full symbol - Paschen formula, open symbols - measurements). This shows that the values are comparable. The vertical lines in Fig. 4 indicate the large-scale regime (low pressure) and the small-scale regime (high pressure) for pressures corresponding to Fig. 3.

The minimum critical breakdown field strength varies between 10^7 V/cm at high atmospheric pressures and 10^{-7} V/cm in low pressure regions where $p_{\text{gas}} = 10^{-12}\text{ bar}$. The breakdown fields on Earth (at sea level) and in Jupiter are $\sim 10^4 \dots 10^6\text{ V/cm}$ which correspond to the values at 1 bar in Figs. 4 and 5. The dependence on the local gas

composition introduces an uncertainty of one order of magnitude as demonstrated in Fig. 4.

Figure 5 shows a close-up of Fig. 4 showing the minimum breakdown field using the data for the different solar system planets in comparison with the two most different examples of gas phase composition (CO_2 and He gas). The results for the solar system planets sit between a pure H_2O (upper limit) and a pure H_2 atmosphere (lower limit).

We note further that values measured for the onset of coronal discharges on a treeless plot of grass are about 3 orders of magnitude lower (40 V/cm; MacGorman & Rust 1998) than the respective value at 1 bar in Figs. 4, 5. MacGorman & Rust (1998) also point out that point discharges from ice crystals which are dominated by their surface (rather than bulk) conductivity, seem likely in thunderstorms for a field strength $> 400 \text{ kV/m}$ ($4 \cdot 10^3 \text{ V/cm}$) which is still ~ 2 orders of magnitude lower than the classical values in Figs. 4 and 5.

Therefore, our results suggest that electrical breakdown can readily occur in cloudy atmospheres of Brown Dwarfs and giant gas planets.

3.2. How many charges are needed for an electric field breakdown?

Laboratory measurements of grain charges suggest that single grains can carry $10^3 - 10^5 \text{ e/grain}$. This is supported by experiments on photoelectrical charging of dust in a vacuum (Sickafoose et al. 2000; metals and glass), grain levitation (Fortov et al. 2001), measurements of graupel on Earth (Lamb & Verlinde 2011), and wind-driven entrainment of Martian dust (Merrison et al. 2012; silicates and iron oxide). Somewhat higher charge loads are suggested from dust-dust collision experiments (e.g. contact electrification and tribo-electrification) with silicate granules by Poppe, Blum & Henning (2000) resulting in 10^{-5} C/m^{-2} (i.e., $\sim 5 \cdot 10^6 \text{ e/grain}$ for $a=1.2\mu\text{m}$), and by volcanic ash experiments involving

dust charging by fractoemission by James et al. (2000) resulting in $10^{-8} \dots 10^{-6.5} \text{C/m}^{-2}$ ($\sim 10^5 \dots 10^{7.5} \text{e/cm}^2$). How do these experimental numbers compare to the number of charges needed to initiate a field breakdown in a substellar atmosphere?

The minimum electric field strength that needs to be overcome in order to produce a field breakdown in an astrophysical gas with a low degree of ionisation (see Fig. 10, upper panel, solid lines) varies only by one order of magnitude between gases of different molecular composition for a given gas pressure. Furthermore, the breakdown voltage measured above thunderclouds on Earth is up to two order of magnitude lower than the classical breakdown values that were discussed here so far (see also the discussion at the end of Sect. 3.1). Keeping these uncertainties in mind, we continue with studying how many charges are needed to initiate a field breakdown in a gas of a given composition for the minimum breakdown voltage $V_{\text{t,min}}$.

The assumption of a spherically symmetric charge distribution (Eq. 6) allows a first order-of-magnitude study, although neither clouds nor cloud particles are truly spherical. Equation 6 is a general expression which allows us to distinguish between these two scale regimes of clouds and grains later on. With the radial distance from a charge distribution of Q_{crit} charges set to the minimum distance for breakdown, d , it follows that

$$Q_{\text{crit}} = 4\pi\epsilon_0 d V_{\text{t,min}} [\text{C}] \quad \Rightarrow Q_{\text{crit}} \propto d \propto \frac{1}{p[\text{Pa}]} \quad (6)$$

1 electron carries only the tiny fraction of a Coulomb: $1\text{C} = 6.24150965 \cdot 10^{18} \text{e}$. The surface charge density for a charge distribution of radius r (grain radius or cloud radius) is given by $\sigma = Q/(4\pi r^2)$. Thus, the critical surface charge density for breakdown is

$$\sigma_{\text{crit}} = \frac{\epsilon_0 d V_{\text{t,min}}}{r^2} = \epsilon_0 E_{\text{r,min}} \left(\frac{d}{r}\right)^2 [\text{C/cm}^2] \quad (7)$$

($\epsilon_0 = 8.85 \cdot 10^{-12} \text{F m}^{-1}$)⁽²⁾ - vacuum dielectric constant or electric permittivity of free space).

² ϵ_0 is in SI unites F m^{-1} with $\text{F} = \text{As/V}$ (A - Ampere) = C/V (C-Coulomb) = $\text{C}^2/(\text{Nm})$

Note that the proportionality at the right hand side of Eq 6 *only holds if* the radial distance from the charge distribution is set to the minimum distance for breakdown according to the minimum of the Paschen curve (Eq. 3). Note further that the pressure needs to be in SI units [Pa] for Q_{crit} to be in units of elementary charges on the right hand side of Eq. 6.

The charge carrying surface, $4\pi r^2$, of our charge distribution can be the effective surface of a cloud or the surface of a single grain ($r = a$). The total charge carrying surface of the cloud, the effective cloud surface, will be provided by the total surface of the particles that form the cloud, rather than being related to the geometrical cloud radius. On large vertical scales, the cloud particles will settle depending on their masses and sizes. Our stationary cloud formation model suggests a large mean grain size at the lower edge of the clouds and a small mean grain size in the cloud’s top region (Woitke & Helling 2004; Witte, Helling & Hauschildt 2009). Smaller particles will remain suspended for longer in the atmosphere than the more positively charged bigger grains. On small scales, the charge separation needed to build up an electric field is influenced by non-spherical grain shapes and chemical surface inhomogeneities, neither of which is included in our considerations yet. For spheroidal grain growth, we refer to Diver & Clark (1997) and Stark et al. (2006).

Our cloud formation model (Woitke & Helling 2003, 2004; Helling & Woitke 2006; Helling, Woitke & Thi 2008) allows us to link numerically derived cloud properties, like grain sizes, grain number densities, and dust surface, to critical breakdown quantities as evaluated in the previous sections. The solution of the our cloud model in the frame of the radiative transfer code PHOENIX (Hauschildt & Baron 1999) allows to link dust properties and the critical breakdown quantities to the atmospheric temperature and pressure scale of a Brown Dwarf or giant gas planet as result of the DRIFT-PHOENIX model atmosphere simulations (Dehn 2007, Helling et al. 2007a,b; Witte, Helling & Hauschildt 2009).

The moment equations of our kinetic dust formation model (Gail & Sedlmayr 1988,

Dominik et al. 1993, Woitke & Helling 2003) allow us to calculate the total dust surface available per unit volume ($A_{\text{dust}}^{\text{tot}}$), and also the mean surface of a grain ($\langle A_{\text{dust}} \rangle$) depending on atmospheric height (i.e. depending on the local temperature and pressure),

$$A_{\text{dust}}^{\text{tot}} = \sqrt[3]{36\pi} L_2 \text{ [cm}^2\text{/cm}^3\text{]} \quad (8)$$

$$\langle A_{\text{dust}} \rangle = \sqrt[3]{36\pi} L_2 / L_0 = A_{\text{dust}}^{\text{tot}} / n_d \text{ [cm}^2\text{]}. \quad (9)$$

L_0 is the zeroth and L_2 the second moment of the grain size distribution function, respectively (e.g. Helling et al. 2001). Equations 8 and 9 allow us to relate the total number of charges needed for breakdown to the total grain surface per unit volume (upper panel, Fig. 7) and to the numbers of grains (lower panel, Fig. 7) available as follows:

$$\sigma \times A_{\text{dust}}^{\text{tot}} \text{ [e}^- \text{/cm}^3\text{]} \quad - \quad \text{number of charges per total dust surface per gas volume} \quad (10)$$

$$\sigma \times \frac{A_{\text{dust}}^{\text{tot}}}{n_d} \text{ [e}^- \text{/grain]} \quad - \quad \text{number of charges per grain.} \quad (11)$$

Note that the total dust surface, i.e. the total cloud particle surface, is related to the charge carrying surface inside a cloud.

The number of charges required to establish an electric field large enough for a breakdown to occur and subsequently to ionise the ambient gas, depends on the local gas pressure. More charges are needed in the low density (pressure) regime of an atmosphere as for example Fig. 6 demonstrates because of the large maximum breakdown distance (compare Figs. 2, 3). The lowest density layers would require a total of about 10^{20} charges to allow an electron avalanche with a subsequent streamer to develop. The actual number depends to a certain extent on the dominating gas species that is being ionised as in the example for H_2O and CO_2 in Fig. 6. The lower panel of Fig. 6 presents this results in (SI) units of critical charge density, $\sigma_{\text{crit}} \text{ [C/cm}^2\text{]}$, assuming that the charges would be located on the grains of the size of the local mean grain size, hence $r = \langle a(T, \rho_{\text{gas}}) \rangle$. Artificially increasing the radius of the charge carrying surface to $r = 100 \times \langle a(T, \rho_{\text{gas}}) \rangle$ (long dashed

red line) verifies the anticipated result of a decreasing critical charge density with increasing surface area that would allow an electric field breakdown.

Figure 7 (upper panel) shows the critical number of charges, $\sigma_{\text{crit}} \times A_{\text{dust}}^{\text{tot}} [\text{e}^-/\text{cm}^3]$, as distributed over the total dust surface per cm^3 of atmospheric gas depending on altitude (represented by the local atmospheric gas pressure). The dust surface is provided by a large number of large dust grains at higher pressure and by small number of smaller grains at lower pressures at the cloud top. If the same total dust surface would be provided by grains of a constant size of 10^{-3}cm (brown long-dash short dash line), the critical number of charges per cm^3 would decrease by more than 5 orders of magnitude.

The lower panel of Fig. 7 shows the critical number of charges per grain, $\sigma_{\text{crit}} \times \frac{A_{\text{dust}}^{\text{tot}}}{n_d} [\text{e}^-/\text{grain}]$, which takes into account the total dust surface and the number of grains present throughout the cloud. Each grain has to carry considerably less charge at the bottom of the cloud compared to the cloud top as here more grains are available. Due to gravitational settling, most of the grains are contained in the deeper cloud where the number of grains is much higher than at the cloud top.

Our results suggest that many charges per grain are required to initiate a breakdown discharge in the upper part of the clouds in Brown Dwarfs and giant gas planets. Such a height-dependent charge distribution results because we apply our results for the maximum breakdown distance, d , which is rather large at the cloud top as demonstrated in Figs. 2, 3. The breakdown distance can, however, decrease by e.g. turbulent or other non-local wind processes which are not taken into account here. A decreasing number of charges needed to initiate an electric field breakdown would then result. Additionally, the charge density, σ , depends on the radius of the charge carrying surface, r . Therefore, we again assess our results for r larger than $\langle a \rangle$, but now by using a constant grain size of 10^{-3}cm (brown long-dash short dash line) throughout the cloud. The comparison with the experiments

with mono-disperse grain ensembles as performed by Sickafoose et al. (2000; green star in Fig. 7), Fortov et al. (2001; magenta vertical bar in Fig. 7), Merrison et al. (2012; blue box in Fig. 7), Poppe, Blume & Henning (2000; blue asterisk in Fig. 7), James et al (2000; blue asterisk in Fig. 7), and values for graupel on Earth from Lamb & Verlinde (2011; orange vertical bar in Fig. 7) suggest that our results for mineral clouds are not unreasonable, especially if we allow that cloud particle sizes can be larger than the mean grain size from our dust model. Such a deviation from the mean grain size is to be expected as our study of the grain size distribution in Helling, Woitke & Thi (2008) demonstrates. Furthermore, critical breakdown field strengths applied here are upper values as experiment on Earth thunderstorms suggest and can, hence, be expected to be 1-2 orders of magnitude lower with the corresponding decreasing effect on the necessary number of charges. The chemical richness of the mineral clouds in the atmosphere of Brown Dwarfs and giant gas planets may introduce further uncertainties compared to the laboratory experiments cited above. The actual material composition may influence the charge distribution on the grain surface leading, for example, to further polarisation effects of the cloud particles. The question of how many charges a dust grain can carry before it is destroyed by the electrostatic stress will be addressed in a forthcoming paper.

Trends with T_{eff} and metallicity $[M/H]$: The quantities that determine if the streamer mechanism occurs and with which efficiency it does so, are determined by the local gas pressure because the gas pressure determines the mean free path of the seed electrons inside the gas of Brown Dwarfs and planets in the electric field. Global quantities that determine an atmosphere’s pressure structure are the effective temperature, T_{eff} , the metallicity, $[M/H]$, and the surface gravity, $\log(g)$, of the object, in the case of non-irradiated objects. The influence of the surface gravity has already been shown in Figs. 6 and 7. We use the surface gravity to distinguish between Brown Dwarfs ($\log(g)=5.0$) and giant gas planets

($\log(g)=3.0$).

Figures 8 and 9 show the influence of T_{eff} and $[M/H]$, respectively, for a small number of DRIFT-PHOENIX models. The metallicity $[M/H]$ is given relative to the solar abundances, hence, $[M/H]=-3.0$ stands for the initial element abundances being decreased by 10^{-3} compared to the solar values. The lowest panels in both figures demonstrate how the DRIFT-PHOENIX temperature-pressure profiles change with changing metallicity. The local pressure mainly increases for a given local temperature for an increasing T_{eff} (Figures 8), while the upper atmospheric parts of the $(T_{\text{gas}}, p_{\text{gas}})$ -structures stay relatively comparable with decreasing metallicity for given T_{eff} and $\log(g)$. The inner atmospheric regions, however, show an increasing gas pressure with decreasing metallicity for a given gas temperature.

The critical charge number density needed to initiate the occurrence of streamers that subsequently might lead to lightning, does change by up to 4 orders of magnitude for a given gas pressure amongst the models of varying effective temperature that form dust clouds. Note that the $T_{\text{eff}} = 2800\text{K}$ -model in Fig. 8 is too hot for dust condensation processes to be efficient. The metallicity of the atmospheric gas has a larger impact on the local temperature. Figure 9 shows that the critical charge number density can differ in the low-metallicity cases much more than for varying T_{eff} . Note that the dust surface available to host the charges does vary amongst the models, with the largest differences occurring again for changing metallicities in the lowest metallicity cases (dashed/dotted line) compared to the solar case (solid line). All models, however, exhibit a comparable total dust surface in the inner, denser regions at the bottom of the cloud. Witte et al. (2009) demonstrated that low-metallicity atmospheres can produce larger dust grains at the inner edge of the cloud than in the solar case if $[M/H] \geq -4.0$.

3.3. Number of electrons vs. number of grains

So far, we have studied the breakdown conditions utilising classical arguments and laboratory measurements assuming that the gaseous atmosphere would have enough free electrons available for starting the electric breakdown process. But, is the number of thermal electrons large enough in Brown Dwarf and giant gas planet atmospheres to provide the seed electrons that are needed to start an electron avalanche in the electric field, for example between two passing grains? The investigation of this question allows us to estimate the efficiency with which streamer discharges could occur inside Brown Dwarf and giant gas planet atmospheres. Streamer discharges are the starting point for large-scale phenomena like lightning that may be followed by a sprite into the less dense atmosphere above.

We compare the degree of thermal ionisation, $\chi_{\text{e,thermal}} = n_{\text{e,thermal}}/n_{\text{H}}$ (solid lines), with the number of dust grains per hydrogen, $n_{\text{d}}/n_{\text{H}}$ (dashed lines) in Fig. 10 (top panel), and we use these two quantities to estimate an efficiency of streamer initiation in a mineral cloud by calculating the ratio $n_{\text{e,thermal}}/n_{\text{d}}$ (Fig. 10, bottom panel). Hence, this efficiency would be the number of streamers per grain pair if each of the thermal electrons in the electric field of two charged grains would initiate an electron avalanche. In the previous section, we have evaluated the conditions under which such a field breakdown can occur.

Figure 10 shows that the efficiency, $n_{\text{e,thermal}}/n_{\text{d}}$, varies with height as at some height the dust number density can have a local maximum while the number of thermal electrons is a rather smooth function of gas pressure which is linked to the gas temperature by the underlying atmosphere model. Hence, the number of electrons available for each colliding pair of charge-carrying grains decreases as shown in the lower panel of Fig. 10. Here, more than one electron would be available for initiating the avalanche process for all pressures above the solid black, horizontal lines ($n_{\text{e,thermal}} = n_{\text{d}}$), and less than one electron would

be available below this line. In both cases, the Brown Dwarf atmosphere (brown) and the giant gas planet’s atmosphere (red), the efficiency of streamer initiation would vary between 1 and $\approx 10^{-5}$. $n_{\text{e,thermal}}/n_{\text{d}} = 1$ means that one streamer per grain pair sets off, and $n_{\text{e,thermal}} < n_{\text{d}}$ means that not every grain pair can initiate a streamer event. To generalise, we can distinguish two regimes regarding the streamer efficiency in a cloud forming atmosphere, the occurrence of which can be less homogeneous if the whole grain size distributions for each atmospheric layer are taken into account,

$$\begin{array}{lll} n_{\text{e,thermal}} > n_{\text{d}} & \text{electron dominated} & n_{\text{e,thermal}}/n_{\text{d}} \gg 1 \\ n_{\text{e,thermal}} < n_{\text{d}} & \text{dust dominated} & n_{\text{e,thermal}}/n_{\text{d}} \leq 1 \dots 10^{-5}. \end{array}$$

The consequence is that the discharge process in cloudy atmospheres will be determined by two populations, the population of the cloud particles and the population of free electrons, respectively. Both populations need to be abundant enough to allow discharge processes to develop into streamers as the pre-condition for the occurrence of lightning.

3.4. An estimate of electron enrichment of the gas phase by dust-dust induced streamer events in mineral clouds

The empirical formula

$$\alpha = Ap \exp\left(\frac{-Bp}{E}\right) \Rightarrow \alpha(E_{\text{min}}) = \frac{Ap}{e} \quad (12)$$

for Townsend’s ionisation coefficient, α [cm^{-1}], enables us to provide first estimates of the number of electrons created when a electron avalanche starts that might develop into a streamer. Streamers are discussed to be a likely possibility to initiate lightning (see Sect. 5.4. in MacGourman & Rust 1998). α is the number of ionisation events performed by an electron in a 1cm path along an electric field. This interpretation is only true if we

assume that the electron undergoes ionisation collisions only for high values of E/p and moderate electron energies (Raizer 1991). The constants A and B are the same constant given in Table 1 for approximating experimental curves. αd would then be an estimate for the number of electrons produced if the electron avalanche would stretch along the whole critical breakdown distance d (compare Fig. 2). The total number of non-thermal electrons per unit time, $N_e^{\text{aval}}[s^{-1}]$, produced by all possible seed electrons that lead to an electron avalanche, can be approximated by

$$N_e^{\text{aval}} \approx f_{\text{eff}} \times \alpha d \times \nu_{\text{coll}}^{dd}(z) \quad (13)$$

$$\approx \frac{n_{\text{e,thermal}}}{1/2 \cdot n_d} \times \alpha d \times \nu_{\text{coll}}^{dd}(z), \quad (14)$$

with $\nu_{\text{coll}}^{dd}(z)$ the frequency of dust-dust collisions at each height z in the atmosphere as derived in Eq.17 in Helling, Jardine & Mokler (2011). Following from Sect. 3.3, we define $f_{\text{eff}} = n_{\text{e,thermal}}/(1/2 \cdot n_d)$ which provides an estimate of the efficiency with which an avalanche could occur. $f_{\text{eff}} > 1$ suggests a superposition of avalanches that are each started by one gas-phase electron.

An electron avalanche can turn into a self-propagating ionisation front by the subsequent development of a streamer in its positively charged wake. This instability can trigger much larger plasma-channel structures like sprites above thunderclouds or lightning bolts below and inside a cloud which we are not considering for our estimate here. The elementary streamer alone, however, results in a number of local non-thermal electrons much larger than predicted by the classical Townsend breakdown by electron avalanche (Eq. 12). Numerical experiments suggest the production of $10^{12} \dots 10^{13}$ electrons per streamer event (e.g. Dowds et al. 1993). Multiple streamers develop if more than one electron is ‘seen’ by a pair of charged grains or two otherwise oppositely charged charge distributions. This efficiency depends on the number of free electrons that are already present in the gas before a streamer-triggering electron avalanche develops and has been derived in Sect. 3.3. For

a streamer breakdown, the number of non-thermal electrons produced during a collisional approach of two dust particles that occur with the frequency $\nu_{\text{coll}}^{dd}(z)$,

$$N_{\text{e}}^{\text{streamer}} = \frac{n_{\text{e,thermal}}}{1/2 \cdot n_{\text{d}}} \times 10^{12} \times \nu_{\text{coll}}^{dd}(z). \quad (15)$$

Given the different nature of an electron avalanche and a streamer, the electron production occurs with a different efficiency. The result is that $N_{\text{e}}^{\text{streamer}} \gg N_{\text{e}}^{\text{aval}}$ (Fig. 11). Our results in Fig. 11 suggest further that the largest impact of the streamer electrons on the local chemistry could be expected in the inner, denser cloud regions in Brown Dwarfs and giant gas planets.

4. Conclusions

Discharge process require a) charge separation on cloud particles and b) a charge separation over large distances to allow large-scale discharges such as lightning or sprites to occur. The laboratory experiments (Poppe, Blum & Henning 2000, James et al. 2000, Fortov et al. 2001, Lacks & Levandovsky 2007, Forward et al. 2009, Merrison et al. 2012) for a variety of minerals (including Martian and volcanic minerals), for graupel on Earth (Lamb & Verlinde 2011), as well as our own investigations (Helling, Jardine, Mokler 2011) suggest that mineral cloud particles will be charged. Mineral cloud particles settle gravitationally in Brown Dwarfs and giant gas planets such that a large scale charge separation can occur inside these clouds. Convection serves as an additional large-scale charge separation mechanism. If small grains are indeed more negatively charged than large grains as suggested by experiments (Hatakeyama & Uchikawa 1952, Kikuchi & Endoh 1982, James et al. 2000, Merrison et al. 2012), spatial charge separation will occur on a large scale by gravitational settling but also on small scales by particle size effects alone. Our investigations of the minimum distance that two charge distributions need to

have for a electric field breakdown to occur (Fig. 2) suggest that small-scale discharges should be expected in high-pressure regions of an atmospheric cloud. Large-scale discharge processes should occur in the upper, low-pressure part of the cloud. This is consistent with observations from Earth where, for example, sprites develop into the low-pressure part of the atmosphere above a thunder-cloud event.

The critical electric field strength to be overcome for a field breakdown varies between 10^7 V/cm at high atmospheric pressures and 10^{-7} V/cm in the upper atmosphere where the gas pressure is low. The critical number of charges per total dust surface per cm^3 change from 10^{23} e/cm³ in the inner atmosphere to $< 10^5$ e/cm³ in the low pressure atmosphere. These numbers compare well with experimental values at the 1bar-pressure level. The number of charges needed to initiate the occurrence of streamers that subsequently might lead to lightning, does not change substantially amongst the atmosphere models of varying effective temperature that form dust clouds. The critical number of charges has the same trend in the low-metallicity cases as for varying effective temperatures.

Generally, a population of charged cloud particles and enough free electrons are needed to allow transient luminous events to occur in extraterrestrial, cloudy atmospheres. The ratio of both determines the efficiency with which discharge events may occur. The rate of electron enrichment is highest in the high-pressure part of the cloud as here, according to our model, a larger charge-carrying surface is available. This is where we expect small-scale discharges to dominate.

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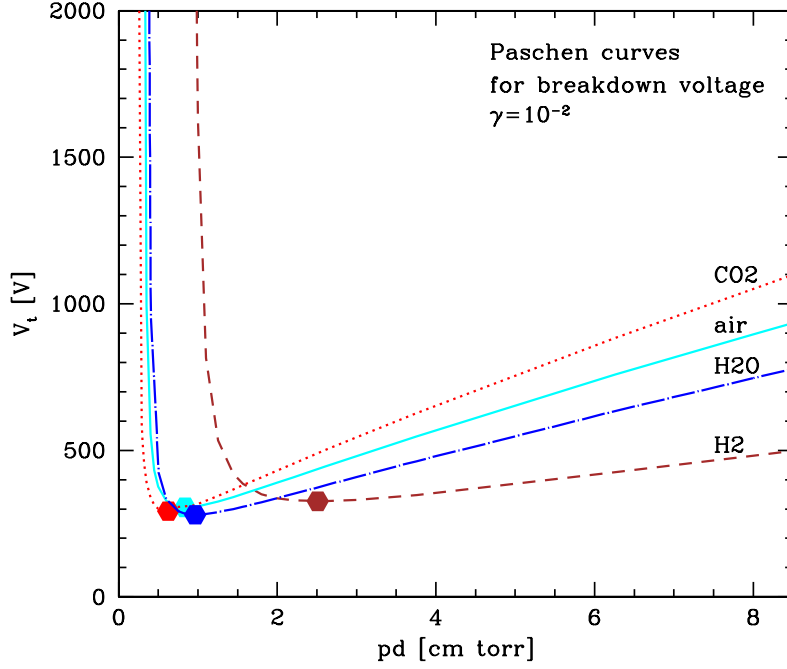


Fig. 1.— The Paschen curve shows the dependence of the breakdown voltage, V_t [V] on the product of gas pressure, p , and the minimum breakdown distance, d , for four molecular gases composed of H_2 , H_2O , CO_2 , and of air. The classical Paschen curve depicted here, has a minimum (indicated by the symbol; Stoletow point) which we use to determine the minimum electric breakdown field in Brown Dwarf and exoplanetary atmospheres in Figs. 2- 3

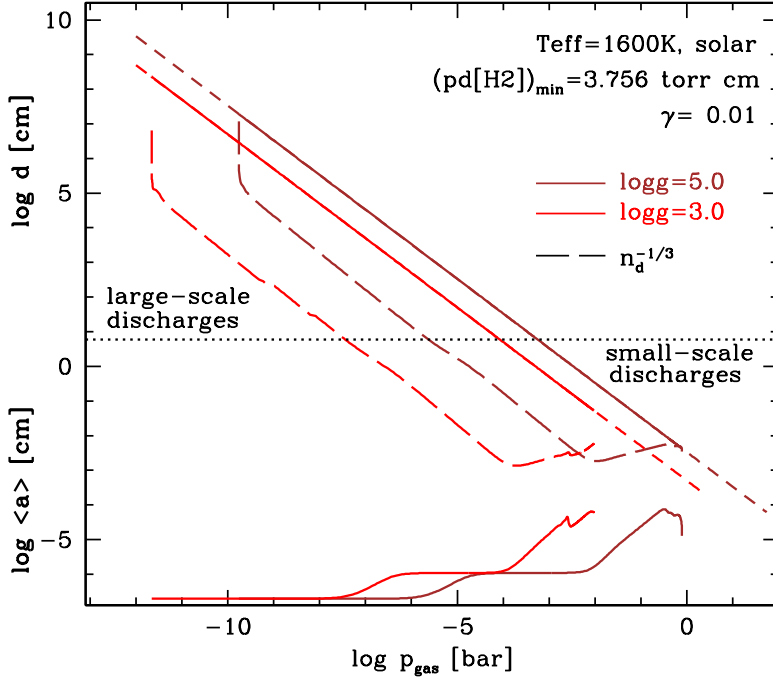


Fig. 2.— The minimum separation of charges of two capacitor plates (representing our charge carrying surfaces like on clouds or on grains) required for discharge (solid and short-dashed in the upper part of the plot). The distance d corresponds to the Paschen minimum where $p_{\text{gas}} \cdot d = 2.509$ torr cm ($=5007 \text{ dyn/cm}^2 \text{ cm}$) for an H_2 gas. Note, an artificial offset between the $\log(g)=5.0$ (brown, "log $g=5.0$ ") and the $\log(g)=3.0$ (red, "log $g=3.0$ ") was applied; all curves should lie on top of each other without this offset. $p_{\text{gas}} \cdot d$ is a constant for a given $A [\text{cm}^{-1} \text{ torr}^{-1}]$ and γ , hence, the same for all atmospheres of the same chemical composition. In this plot, an H_2 -gas is assumed for which $A[\text{H}_2]=5 \text{ cm}^{-1} \text{ Torr}^{-1}$ (Raizer 1991) and Townsend's 2nd ionisation coefficient $\gamma = 0.001$ is used. The solid lines show the pressure interval where clouds form and the dashed lines show the whole atmospheric pressure range modelled. Raizer (1991) notes that discharge sparks set in if the plate distance is $>6\text{cm}$ (horizontal dotted line) which helps us here to distinguish between large-scale and small-scale discharges. We overplot two more length scales for comparison: The dust-dust mean free path $n_d^{-1/3}$ (long dashed lines) and the mean grain sizes, $\langle a \rangle$, at the bottom of the plot.

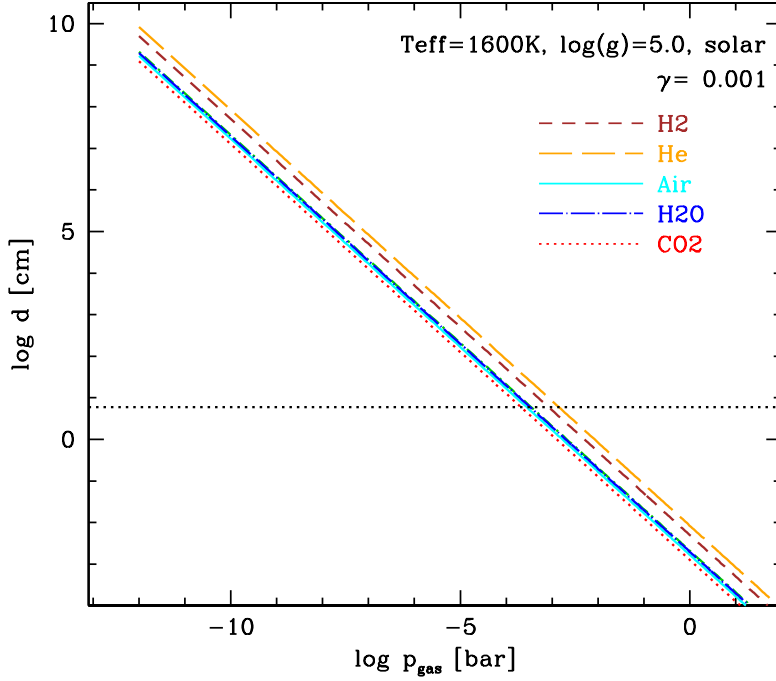


Fig. 3.— Dependence of breakdown distance d at the Stoletow point on the composition of the ionised gas. The variation in these distances for 6 cases (H_2 , He, air, H_2O , CO_2 ; Table 4.1 in Raizer 1991) shows that the uncertainty resulting from atmospheric composition is a factor of 10. This estimate also covers differences in A depending on the pressure regime in which the measurements were made (high [~ 1 bar] vs. low pressure; Table 7.1 in Raizer 1991). Sentman (2004) has published data for mixed gases but the lack of a consistent notation makes application difficult.

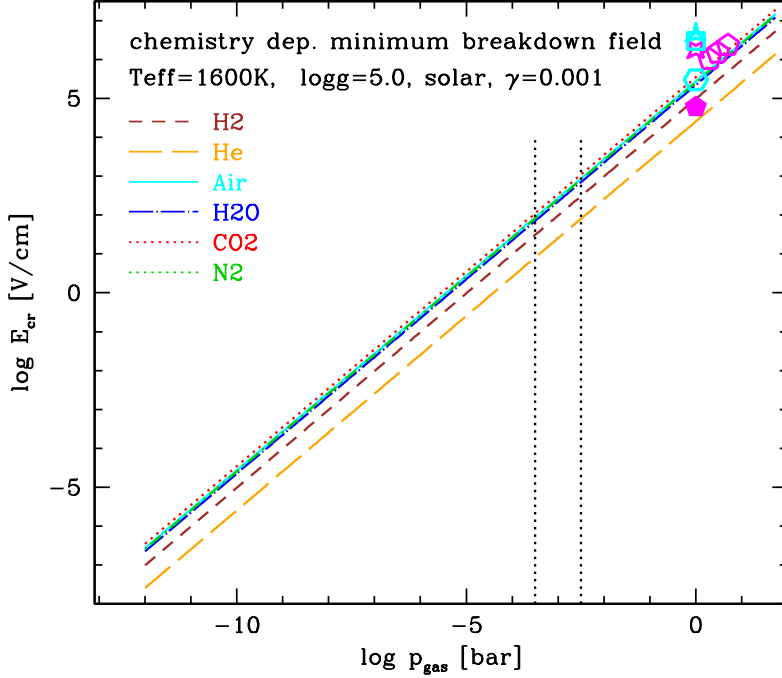


Fig. 4.— The minimum critical breakdown electric field corresponding to the minimum of the Paschen curve for individual ionised gases (H_2 , He, air, H_2O , CO_2 ; Table 4.1 in Raizer 1991). Pressures higher than indicated by the vertical dotted line correspond to $d < 6\text{cm}$, and pressures lower than indicated by the vertical dotted line correspond to $d > 6\text{cm}$ according to Fig. 3. (This set of dotted double lines results from the intersection interval of the dotted line in Fig. 3.) The symbols indicate the breakdown field for Earth (cyan) and Jupiter (magenta) as given in Yair et al. 1997 (Table 1; open symbols: measured, solid: with drops and ice, stars: theoretical estimate).

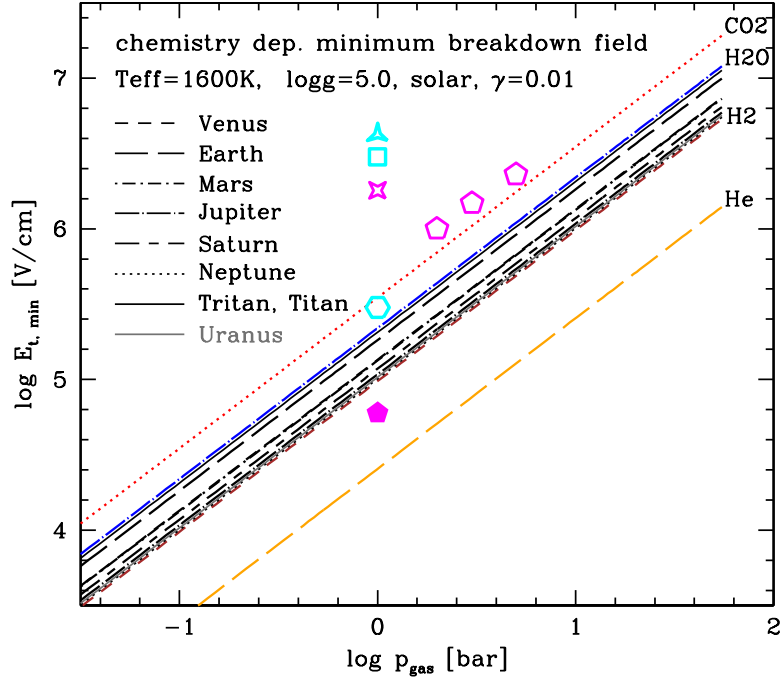


Fig. 5.— The minimum critical breakdown electric field for a Brown Dwarf atmosphere with $T_{\text{eff}} = 1600\text{K}$ and $\log(g)=5.0$ assuming that the field break down happens in different gas compositions. This is a zoom into Fig. 4 for CO_2 (red dotted), H_2O (blue long-dashed), H_2 (brown dashed) and He (orange long dashed) with the curves assuming the solar system planetary atmosphere compositions over-plotted in black. The curve for Uranus and Neptune lie almost on top of each other.

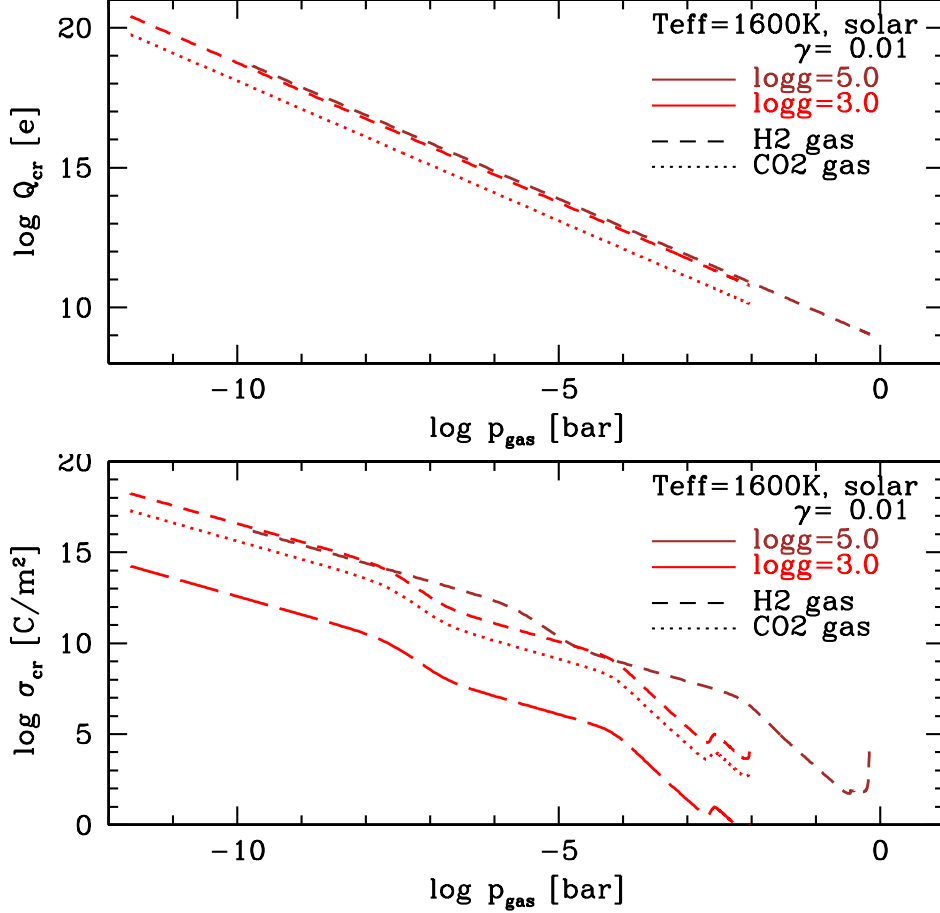


Fig. 6.— **Top:** The total number of charges needed to overcome the breakdown field (Eq. 6) for a H_2 dominated gas in a mineral cloud in a brown dwarf atmosphere (brown) and a giant gas planet (red). These charges are assumed to exist on two charge-carrying surfaces separated by the minimum distance for discharge. The case of a CO_2 -dominated atmosphere is over-plotted for the giant-gas planet (dotted line). **Bottom:** The critical surface charge density, $\sigma_{\text{cr}} = Q_{\text{cr}}/(4\pi r^2)$ critical for an electric field breakdown. σ_{cr} was calculated for $r = \langle a(T, \rho_{\text{gas}}) \rangle$ assuming that all grains are of the size of the local mean grain size, except for the long-dashed line which shows σ_{cr} for $100 \times \langle a \rangle$. Note that $1 \text{ C/m}^2 = 6.24 \cdot 10^{14} \text{ e/cm}^2$.

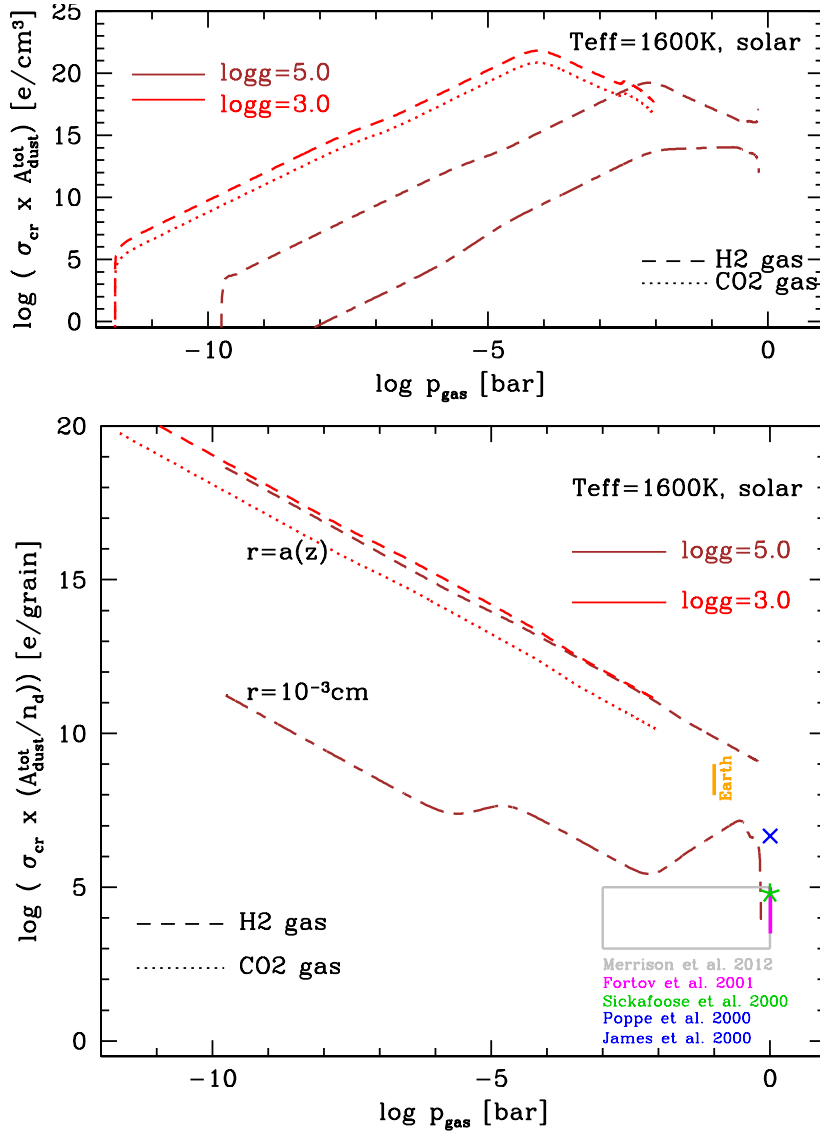


Fig. 7.— Critical number of charges needed for electric breakdown in mineral clouds inside atmospheres for objects with $T_{\text{eff}}=1600\text{K}$ and $\log(g)=3.0$ (red) and $\log(g)=5.0$ (brown). **Upper panel:** The charges on the total dust surface $A_{\text{dust}}^{\text{tot}}$ per cm^3 of atmospheric gas as $\sigma_{\text{cr}} \times A_{\text{dust}}^{\text{tot}} [\text{e}/\text{cm}^3]$. **Lower panel:** The number of charges per dust grain $\sigma_{\text{cr}} \times (A_{\text{dust}}^{\text{tot}}/n_d) [\text{e}/\text{grain}]$. The symbols represent the following data sources: grey rectangle – Merrison et al. (2012), magenta vertical bar – Fortov et al. (2001), green asterisk – Sickafoose et al. (2000), blue cross – Pope et al. (2000) and James et al. (2000), orange vertical bar – values for Earth hale from Lamb & Verlinde (2011).

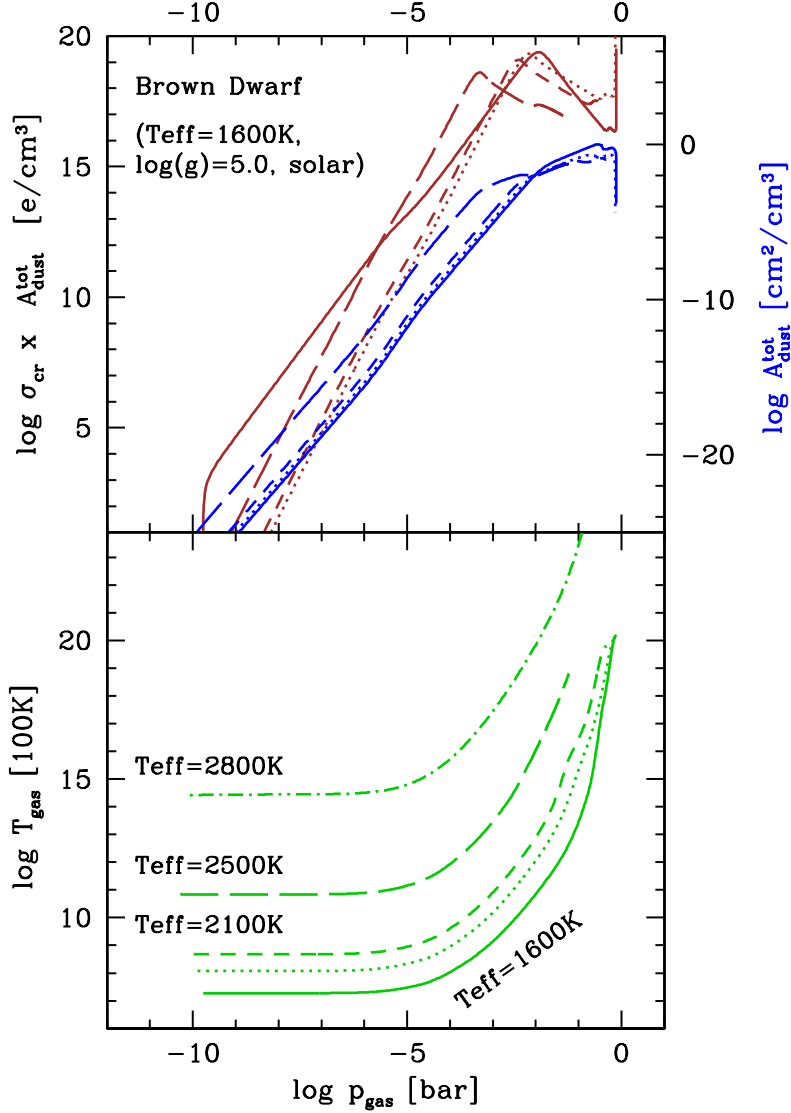


Fig. 8.— Critical charge number density, σ_{cr} [e/cm³] per total dust surface needed to overcome the local breakdown field depending on the effective temperature of the object (top panel). The results are plotted for 5 solar-metallicity Brown Dwarf model atmospheres ($\log(g)=5.0$) with $T_{\text{eff}} = 1600\text{K}$ (solid), 1900K (dotted), 2100K (short dashed), 2500K (long dashed), 2800K (dash-dot). The lower panel (local gas temperature) demonstrates why the critical surface charge density $\sigma_{\text{cr}}(p)$ changes for different effective temperatures.

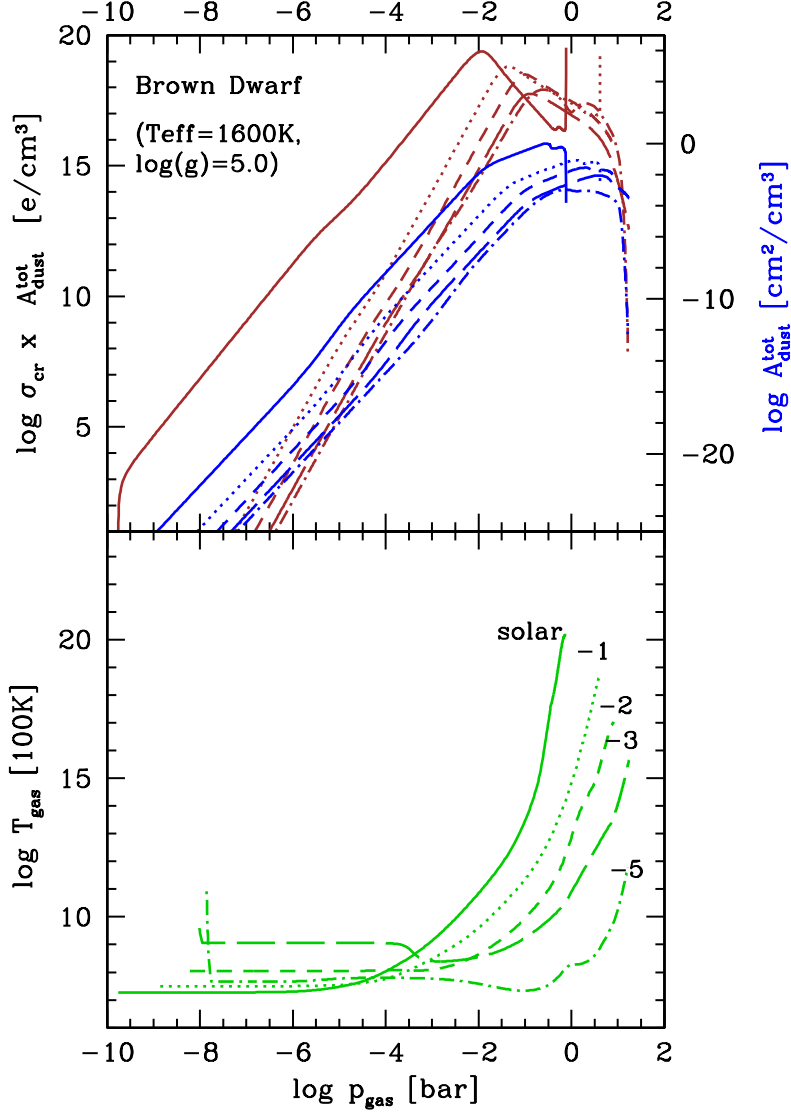


Fig. 9.— Critical charge number density, σ_{cr} [e/cm³] per total dust surface, needed to overcome the local breakdown field depending on the metallicity of the object (top panel). The results are plotted for 5 Brown Dwarf model atmospheres ($\log(g)=5.0$) with different metallicities $[M/H]=0$ (solar, solid), -1 (dotted), -1 (short dashed), -3 (long dashed), -5 (dash-dot). The lower panel (local gas temperature) demonstrate why the critical surface charge density $\sigma_{\text{cr}}(p)$ changes for different $[M/H]$.

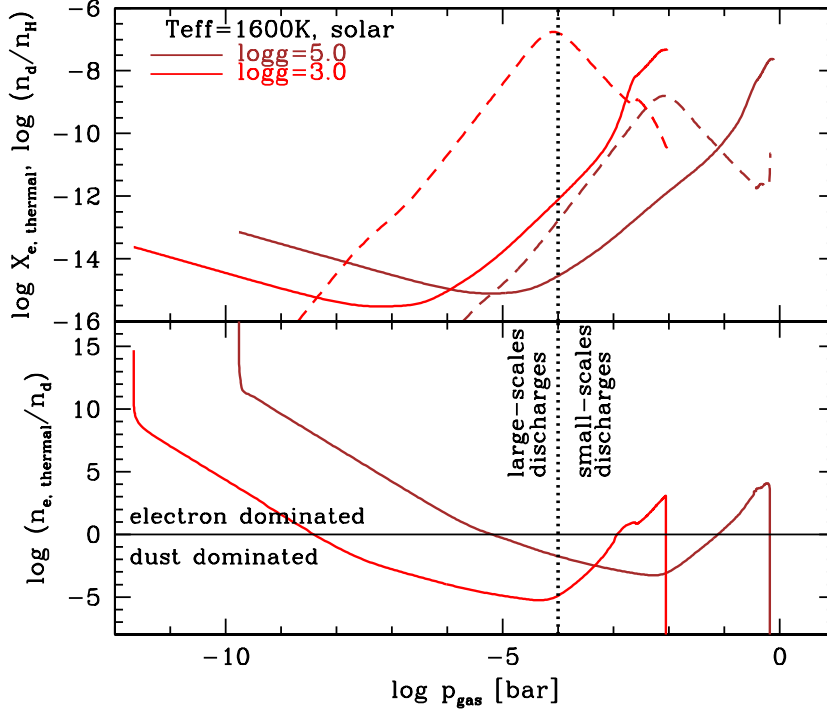


Fig. 10.— The efficiency of discharges in planetary atmospheres with mineral clouds. **Top:** Degree of thermal gas ionisation, $\chi_{\text{e, thermal}} = n_{\text{e}}/n_{\text{H}}$ (solid lines), and the dust number density per hydrogen, $n_{\text{d}}/n_{\text{H}}$ (dashed lines), for a Brown Dwarf and a giant gas planet atmosphere for the same Drift-Phoenix models as in Fig. 6. **Bottom:** The ratio of the number of thermal electrons, $n_{\text{e, thermal}}$, to the number of cloud particles, n_{d} , provides a measure of the efficiency with which a streamer may be initiated in a mineral cloud. Two different regimes appear: above the black line - electron dominated, hence more than one electron is available per grain pair, below the black line - dust dominated, hence less than one electron is available per grain pair. The dotted vertical lines distinguished the cloud regimes of potential large-scale cloud discharges and small-scale, inter-grain discharges similar to Figs. 2 - 4

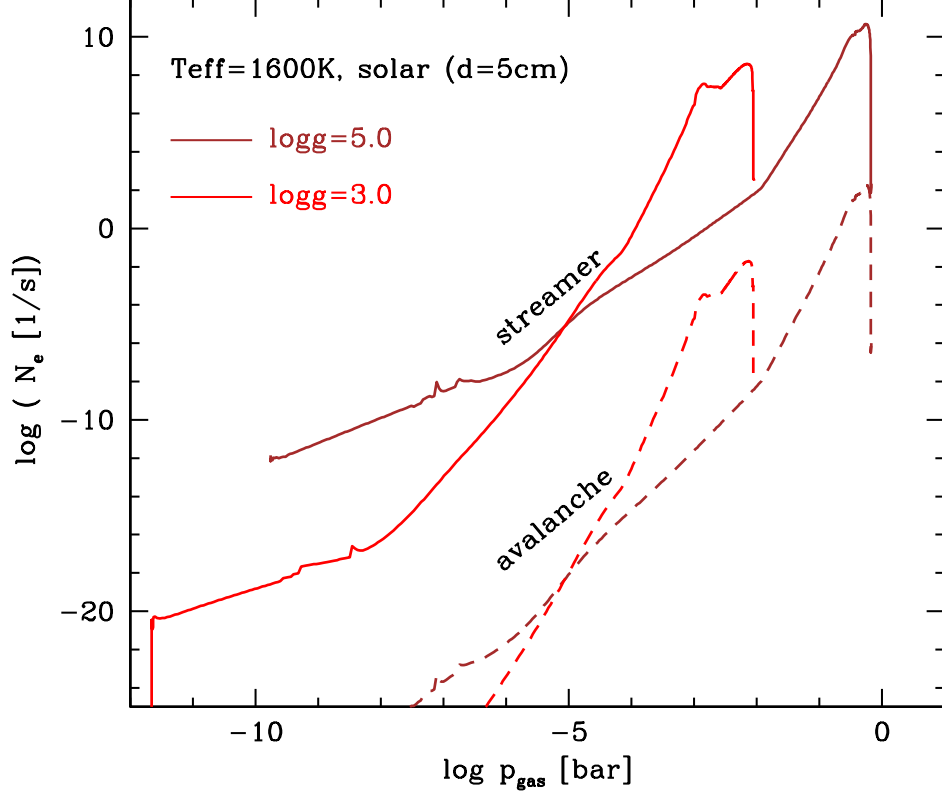


Fig. 11.— Gas-phase enrichment by dust-dust collision triggered discharges. Electron avalanche (dashed lines; $d = 5\text{cm}$ used) yields considerably less free charges than streamer events (solid lines). The same Brown Dwarf (brown) and a giant gas planet (red) atmosphere models are used as in Fig. 10.